

# *E0:227, Program Analysis and Verification*

*3:1, January - April 2009*

*E-Classroom, CSA, M-W 11:30am-1pm*

*<http://www.csa.iisc.ernet.in/~raghavan/pav09/index.html>*

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## *Software development is hard*

Average software-development project [Barry Boehm, ICSE '06 keynote] incurs:

- 90% cost overrun
- 121% time overrun
- delivers only 61% of initially promised functionality

# *Software development lifecycle*

For each release of the software:

Requirements

Analysis and Design

Coding

Testing

Production/deployment; feedback from users

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Testing, finding and fixing bugs (i.e., Quality Assurance) consumes 50% of total cost and time of software development.

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Testing, finding and fixing bugs (i.e., Quality Assurance) consumes 50% of total cost and time of software development.

The problem gets worse after multiple releases, because:

- People lose knowledge of the code
- Code becomes bigger, more complex, and poorer structured

## *Why quality assurance takes so much effort*

- Defects are common
- Are hard to find
  - often, get identified only after release
  - no good tools, and people don't use ones that are there
- When a program crashes, or gives wrong answer, hard to detect the root defect
- Defects in requirements or design should be found before coding starts, else code will manifest it
  - however, no widely used formal techniques for these
- Incorrect understanding of customers requirements

## *Kinds of software defects*

- Crashes
  - Null pointers, uninitialized values
  - Array index out of bounds, buffer overrun
  - Memory leaks
  - Misuse of pointers and buffers (in languages like C)
  - Unreachable code
- Does not interact with other software in the same way as the previous version.
- Leaks information to unauthorized channels
- Performs poorly
- Logical errors (design-time errors)

## *What's wrong with this program?*

```
int middle(int x,
           int y,
           int z) {
    int m = z;
    if (y < z)
        if (x < y)
            m = y;
        else if (x < z)
            m = x;
    else
        if (x > y)
            m = y;
        else if (x > z)
            m = x;
    return m;
}
```



## *What's wrong with this program?*

```
int middle(int x,          ⇒ int middle(int x,
                        int y,          int y,
                        int z) {        int z) {
    int m = z;                      int m = z;
    if (y < z)                       if (y < z)
        if (x < y)                     if (x < y)
            m = y;                       m = y;
        else if (x < z)                 else if (x < z)
            m = x;                       m = x;
    else                               else
        if (x > y)                       if (x > y)
            m = y;                       m = y;
        else if (x > z)                 else if (x > z)
            m = x;                       m = x;
    return m;                          return m;
}
```

Tool BLAST identifies the two lines before `return` as unreachable

## *A common approach to software validation: Testing*

- A test suite (set of test cases) is created, and executed for each version.
- **Black box** testing: Test cases are created manually by user, or generated randomly.
- **White box** testing: Test cases are generated by an analysis of the program code to increase code coverage.
  - Typically needs tool support.
- What's good about testing? *All bugs found are real bugs.*
- What's bad about testing?

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- **Black box** testing: Test cases are created manually by user, or generated randomly.
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  - Typically needs tool support.
- What's good about testing? *All bugs found are real bugs.*
- What's bad about testing?

- 100% coverage of the program's behavior is impossible.
- Therefore, cannot find all bugs or prove the absence of bugs.

- Very hard to test the portion inside the “if” statement!

```
input x
if (hash(x) == 10) {
    ...
}
```

## *Program verification*

The algorithmic discovery of properties of a program by inspection of the source text.

– *Manna and Pnueli, "Algorithmic Verification"*

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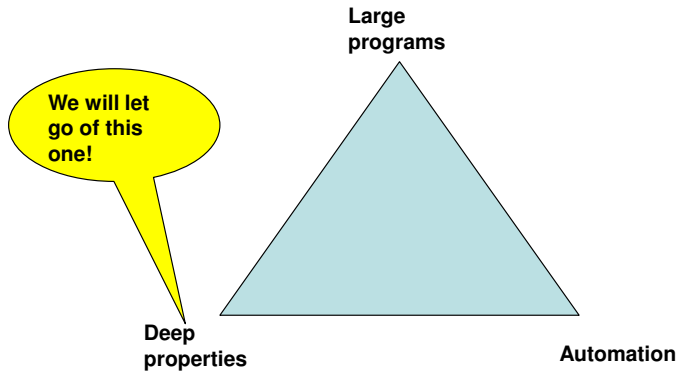
– *Manna and Pnueli, “Algorithmic Verification”*

Also known as: static analysis, static program analysis, formal methods, . . .

## *Difficulty of program verification*

- What will we prove?
  - “Deep” specifications of complex software are as complex as the software itself
  - Are difficult to prove
  - State of the art tools and automation are not good enough
- We will focus on “shallow” properties
  - That is, we will prove “partial correctness”, or absence of certain classes of errors (e.g., null pointer dereferences)

# Elusive triangle



*Example: Determining whether variables are odd (o) or even (e)*

<code>p = oddInput()</code>	<code>(p,o)</code>	
<code>q = evenInput()</code>	<code>(p,o)</code>	<code>(q,e)</code>
<code>if (p &gt; q)</code>	<code>(p,o)</code>	<code>(q,e)</code>
<code>p = p*2 + q</code>	<code>(p,e)</code>	<code>(q,e)</code>
<code>write(p)</code>	<code>(p,oe)</code>	<code>(q,e)</code>
<code>if (p &lt;= q)</code>	<code>(p,o)</code>	<code>(q,e)</code>
<code>p = p+1</code>	<code>(p,e)</code>	<code>(q,e)</code>
<code>write(p)</code>	<code>(p,e)</code>	<code>(q,e)</code>
<code>q = q+2</code>	<code>(p,e)</code>	<code>(q,e)</code>



## *A verification approach: abstract interpretation*

- A kind of program execution in which variables store *abstract* values from bounded domains, not concrete values
- Input values are also from the abstract domains
- Program statement semantics are modified to work on abstract variable values
- We execute the program on *all* (abstract) inputs and observe the program properties from these runs

## *Example: The abstraction*

- Possible values of each variable:  $\{o, e, oe\}$ .
- Modified statement semantics:

+	<i>o</i>	<i>e</i>	<i>oe</i>
<i>o</i>	<i>e</i>	<i>o</i>	<i>oe</i>
<i>e</i>	<i>o</i>	<i>e</i>	<i>oe</i>
<i>oe</i>	<i>oe</i>	<i>oe</i>	<i>oe</i>

*	<i>o</i>	<i>e</i>	<i>oe</i>
<i>o</i>	<i>o</i>	<i>e</i>	<i>oe</i>
<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>
<i>oe</i>	<i>oe</i>	<i>e</i>	<i>oe</i>

## *Example: The abstract interpretation*

### Abstract interpretation

<pre>p = oddInput() q = evenInput() if (p &gt; q)   p = p*2 + q write(p) if (p &lt;= q)   p = p+1 write(p) q = q+2</pre>	<pre>&lt;(p,o)&gt;</pre>
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--	---

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<code>p = oddInput()</code>	$\langle (p,o) \rangle$
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## Example: The abstract interpretation

### Abstract interpretation

<code>p = oddInput()</code>	$\langle(p,o)\rangle$
<code>q = evenInput()</code>	$\langle(p,o), (q,e)\rangle$
<code>if (p &gt; q)</code>	$\langle(p,o), (q,e)\rangle$
<code>p = p*2 + q</code>	$\langle(p,e), (q,e)\rangle$
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<code>q = q+2</code>	$\langle(p,e), (q,e)\rangle \langle(p,o), (q,e)\rangle$

### Ideal results

$(p,o)$	
$(p,o)$	$(q,e)$
$(p,o)$	$(q,e)$
$(p,e)$	$(q,e)$
$(p,oe)$	$(q,e)$
$(p,o)$	$(q,e)$
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$(p,e)$	$(q,e)$
$(p,e)$	$(q,e)$

## Example: The abstract interpretation

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<code>write(p)</code>	$\langle (p,o), (q,e) \rangle \langle (p,e), (q,e) \rangle$
<code>if (p &lt;= q)</code>	$\langle (p,o), (q,e) \rangle \langle (p,e) \mathbf{X}, (q,e) \rangle$
<code>p = p+1</code>	$\langle (p,e), (q,e) \rangle \langle (p,o) \mathbf{X}, (q,e) \rangle$
<code>write(p)</code>	$\langle (p,e), (q,e) \rangle \langle (p,o) \mathbf{X}, (q,e) \rangle$
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## *Another verification approach: Type systems*

- Treat assignment statements as a set of mathematical equations, and program variables as mathematical variables.

$p = \text{oddInput}()$

$q = \text{evenInput}()$

$p = p*2 + q$

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- Let domain of variables be  $\{o, e, oe\}$ . Let operators “\*” and “+” have the meanings as described in tables earlier.
- Solve the set of equations.

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- Let domain of variables be  $\{o, e, oe\}$ . Let operators “\*” and “+” have the meanings as described in tables earlier.
- Solve the set of equations.
- Two solutions for the above equations: (1)  $\langle p = oe, q = e \rangle$ , (2)  $\langle p = oe, q = oe \rangle$ .
  - Solution (1) is more precise than solution (2).

## Comparing abstract interpretation and type systems

- Reminder: The type solution is  $\langle p = oe, q = e \rangle$ .
- Type systems approach is “flow insensitive”: It gives each variable a single value valid at *all* program points, whereas abstract interpretation gives different values at different points.
- The single value is a over-approximation (union) of values at all program points. Therefore, type system approach is *less precise* than flow-sensitive abstract interpretation.
- However, type system approach is more efficient.

Both approaches produce over-approximations of the ideal results. *This is true of verification approaches in general.* In contrast, testing produces an under-approximation of the ideal results.

- In other words, Flow-insensitive verification  $\supseteq$  flow-sensitive verification  $\supseteq$  ideal results  $\supseteq$  testing.



## Overview of PAV course

- Introduction (1 lecture) (*durations are tentative*)
- Specifying semantics of programming language formally. (1)
- Verification approaches
  - Dataflow analysis (7)
  - Abstract interpretation (3)
  - Type inference (8)
  - Assertional reasoning (2)
- Program slicing (6) (*Time permitting*)

## *Flavour of the course*

- Semantics: associating a mathematical function with each kind of statement in the language.
- Dataflow analysis
  - Setting up a set of mathematical equations, and using a kind of graph traversal to solve these equations
  - Proving termination of the approach
- Abstract interpretation and type systems
  - Examples of abstract domains and abstract statement semantics
  - Proving that the results computed are an over-approximation of the ideal results
  - Proving termination of the approach
- Assertional reasoning: A first-order predicate logic for deriving facts about a program

## *Prerequisites*

- Discrete structures such as sets, relations, partially ordered sets, functions
- (Undergraduate level) algorithms
- Mathematical logic (propositional, first-order)
- General mathematical maturity: comfort with notation, understanding and writing proofs
- Familiarity with imperative languages like C
- (Moderate) programming experience

## *What we will not cover*

- Software engineering
  - How to collect requirements from customers and prioritize them
  - Planning and management of software development
  - Design, architecture, coding
- Programming languages
- Analysis of parallel/concurrent programs, distributed systems

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Compilers course offered by Prof. Y. N. Srikant this semester will cover applications of program analysis to compiling, among other topics.

## *Assignments and exams (tentative)*

- Assignments
  - 5-6 assignments
  - Most of them written, some involve coding
  - 50% weight
- Mid-sem exam (20%), End-sem exam (30%)

## Misconduct policy

- Academic misconduct (e.g., copying) will not be tolerated
- Discussion in exams  $\Rightarrow$  automatic fail grade for both students
- Assignments
  - Try to work individually.
  - If you choose to discuss with other students
    - You may discuss only with students registered in the class (or with the Deepak or Raghavan)
    - You must write your answer individually, in your own words. No copying, no looking at the other person's answer!
  - For *each* violation of above policy  $\Rightarrow$  zero for the entire assignment *plus* one grade-point reduction in final grade (for the one who copied).
    - Grade-point reductions over multiple violations will accumulate.
  - **Grading:** Your marks will be based on your written answer *and* on a viva. (There will be a viva for each assignment.)

## *Late policy for assignments*

- 10 “free” late days for use over all assignments.
- For each late day after free days have been exhausted  $\Rightarrow$  25% penalty on the assignment marks. (Weekends and weekdays treated the same.)
- No late days allowed on final assignment.